Influence of van der Waals forces on the waveguide deformation and power limit of nanoscale waveguide devices

Bi-cai Zheng, Wei Luo, Fei Xu,* and Yan-qing Lu†
National Laboratory of Solid State Microstructures and College of Engineering and Applied Sciences, Nanjing University, Nanjing 210093, People’s Republic of China
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The ultrashort-range force, the van der Waals force (VWF), rises rapidly when one nanoscale waveguide (NW) is close to another one, and is stronger than the external transverse gradient force. We theoretically investigate the great influence of the VWF on the device performance in a typical NW optomechanical system consisting of a suspended silicon waveguide and a silica substrate including waveguide deformation stiction and failure mechanism. The device shows unique optically activated plastic and elastic behaviors and stiction due to the VWF. When the input optical power is above the critical power, the waveguide is sticking to the substrate and the deformation is plastic and unrecoverable, even though the total force is less than the yield strength of the waveguide material. This is important and helpful for the design and applications of optomechanical devices.

Optomechanical systems are a burgeoning field that combines nanophotonic and nanoelectromechanical devices seamlessly in an integrated system. Various configurations have been proposed and demonstrated in optomechanical systems including high-finesse cavity with radiation-pressure force [1–3] and evanescently coupled optical nanoscale waveguides (NWs) with the transverse gradient force (TGF). In the evanescently coupled configuration, a transverse gradient force can be generated from the lateral gradient of a propagating light field in NWs [4,5]. The force can be used directly for electromechanical actuation and precisely control the positions of optical waveguides and devices [6–14]. This TGF works with the highly evanescent NW and does not require a reflective surface; thus it is more versatile for future large-scale photonic integrated circuits in planar structures than the radiation-pressure force. So far, a number of devices have been studied for realizing the TGF between a substrate and a suspended waveguide or two parallel waveguides. These devices may find plenty of applications in optical signal processing, which include nonlinear signal processing devices [8], tunable directional couplers [10], tunable birefringence devices [11], wavelength-filtering devices [12], etc.

In order to make as much use of the force as possible, the width of the waveguide and the gap between the waveguides or substrates should be as small as possible. In general, the size is of tens or hundreds of nanometers. Tens of $\mu$N attractive or repulsive force can be achieved at the input optical power of tens of mW [10,11]. A smaller gap between waveguides means a stronger TGF. However, another type of force, the internal force or the van der Waals force (VWF), which is sometimes referred to as the Casimir force in the microelectromechanical system [15–17], arises and can be relatively strong at such small sizes compared to the TGF. The VWF originates from the instantaneous dipole generated by the fluctuation of the electron cloud surrounding the nucleus of electrically neutral atoms [18]. It is an ultrashort-range force and decays rapidly to zero away from the surface. Different from the TGF, the VWF is generally attractive in nature, and has nothing to do with the optical power. In fact the VWF, which is stronger than the TGF at low power, can exist between NWs with a nanoscale gap. In previous work on optomechanical devices, it was easily neglected except for the calculation of the short-range Casimir force between two waveguides [19] and the control of the Casimir force between a photonic-crystal membrane and the substrate [20]. It is important to further study the competition and cooperation between the VWF and the TGF and how the VWF affects the physical geometry and optical and mechanical characteristics in NW-based optomechanical devices. In this paper, we investigate theoretically the contribution from the VWF in the performance of a typical optomechanical device. We calculated the mechanical deformation induced by different forces. The results show that the VWF plays a very important and different role in optomechanical devices.

A significant influence of the VWF is that the waveguide shows distinctive optically activated plastic and elastic behaviors and stiction. When the optical power is relatively low, the waveguide deformation is elastic and can return to its original shape if the optical power decreases to zero. However, there is an elastic limit related to the input optical power due to the existence of the VWF. The waveguide deformation resembles plastic deformation and the waveguide will be permanently bonded to the substrate when the optical power increases beyond the critical value. The phenomenon can occur even though the waveguide material is still in its elastic region. These unique characteristics are important and helpful for the design and operation of optomechanical devices, and would possibly open new routes to many potential applications such as switch and memory.

We consider the typical structure in optomechanical devices as shown in Fig. 1. It is a simple and generic configuration which consists of a silica substrate and a suspended silicon waveguide. The waveguide is designed to separate from the substrate by a gap of size $g$, in the absence of deformation. The suspended section has a length of $L$ and the waveguide has a cross section of dimensions $a \times d$. From previous work [6], it is known that the force on the free-standing waveguide arises when the guided light is evanescently coupled to the dielectric

*feixu@nju.edu.cn
†yqlu@nju.edu.cn
substrate. The magnitude of the force is proportional to the optical power, and the sign is always attractive. On the other hand, strong intermolecular and surface effects give rise to the VWF even without the input power. That force can deform the beam and thus change the effective refractive index.

According to the VWF theory, the potential between two small molecules is purely attractive when the distance between molecules is more than several angstroms \[18\] and two small molecules is purely attractive when the distance \( d \) is greater than the diameter of the molecule and the substrate, and the number density of molecules in the substrate \[18\], respectively. To calculate the force between molecules in the substrate \[18\], respectively. To calculate the Hamaker constant of material 1 and material 2, respectively \[21\]. For pure silica, the Hamaker constant is \( 6 \times 10^{-20} \) J and for pure silicon, the Hamaker constant is \( 1.1 \times 10^{-18} \) J \[22\].

Considering the retardation effect of the VWF at the relatively large separations (>5 nm), the full Lifshitz equation should be applied to calculate the Hamaker constant \[18\]. However, in the gap range in our model (<100 nm), we can use the following simplified equation to calculate the Hamaker constant with the retardation effect: 

\[ A_{\text{ext}} = A_{\text{non-ext}}/(1 + p|g|/100 \text{ nm}) \]

where \( p \) is estimated to be around 10 in our model \[18\].

Then, according to the virtual work principle, we can get

\[ F_{\text{VWF}} = -\frac{\partial w(g)}{\partial g} = -\frac{A_{\text{ext}} a}{6\pi} \left[ \frac{1}{g^3} - \frac{1}{(g + d)^3} \right]. \]  

where \( F_{\text{VWF}} \) represents the VWF per unit length. Using Eq. (2), we can plot the relationship between \( F_{\text{VWF}} \) and \( g \), which can be seen in Fig. 2(a).

For infinitely long waveguides without loss, the TGF can be calculated as follows \[4\]:

\[ f_{\text{TGF}} = -\frac{1}{c} \frac{n_g}{\partial \omega} \left| \frac{\partial g}{\partial \omega} \right| \]  

where \( f_{\text{TGF}} \) represents the TGF per unit length per unit power, \( c \) is the speed of light in vacuum, \( n_g \) is the group index, \( \omega \) is the frequency, and \( k \) is the wave vector. By substituting \( \omega = c k/n_{\text{eff}} \) into Eq. (3), the TGF can be expressed as a function of the effective index \( n_{\text{eff}} \):

\[ f_{\text{TGF}} = -\frac{1}{c} \frac{n_g}{\partial n_{\text{eff}}} \left| \frac{\partial g}{\partial n_{\text{eff}}} \right| \]  

Using Eq. (4), we can plot the relationship between \( f_{\text{TGF}} \) and \( g \) when the wavelength is fixed at 1550 nm, which can be seen in Fig. 2(b).

From the figures above, the VWF increases more rapidly than the TGF when the gap declines to zero. It can roughly be estimated that when the optical power is around 0.5 mW and the gap is around 80 nm, the VWF and the TGF have the same order of magnitude. To further investigate the relationship between these forces, a new function can be defined as

\[ F(P, g) = |f_{\text{TGF}}| - |F_{\text{VWF}}|. \]

where \( P \) is the optical power, and \( f_{\text{TGF}} \) and \( |F_{\text{VWF}}| \) are the absolute values of the TGF and the VWF. The calculated results are plotted in Fig. 2(c). The figure shows that when optical power is low and the gap is small (the lower left area of the figure), the VWF is comparable with or even much larger than the TGF, which indicates that the VWF cannot be neglected and even dominates under this circumstance. The balanced...
If we want to get an accurate solution, a numerical iterative feedback tuning method has to be employed; it will be discussed in the following paragraphs. Here we try to obtain the approximate solution by a simplified averaged-force method. We firstly consider the simplest case of a uniform load, and then an analytical solution can be given:

$$u(x) = -q_0 x^2(x - L)^2/24EI = -D_{max}(2/L)^4x^2(x - L)^2.$$  

(7)

The $D_{max}$ occurs at the center of the waveguide. By slightly transforming Eq. (7), we can get $q_0 = 24EI(2/L)^4D_{max}$. We can find the linear relationship between the assumed uniform load $q_0$ and the $D_{max}$, which is shown in Fig. 3 (the solid black line). Here the designed gap between the waveguide and the substrate is fixed at 80 nm and the length of the waveguide is 30 $\mu$m. We can calculate the $D_{max}$ if the load is beyond the yield strength of the waveguide material \[24\] and the result is much larger than 80 nm.

On the other hand, the averaged force can be calculated by integrating both the VWF and the TGF along the given shape, which is decided by $D_{max}$ using the equation $u(x) = -D_{max}(2/L)^4x^2(x - L)^2$. The averaged forces (VWF + TGF) of various optical powers are shown in Fig. 3(a) (the dashed colored lines).

There are two intersections between the solid black line and one dashed colored line at low optical power. The right intersection with larger $D_{max}$ corresponds to an unstable equilibrium state. At the left intersection with smaller $D_{max}$, a stable equilibrium state with such a force can be realized by the VWF and the TGF at corresponding optical power. This is an approximate solution. The intersection A in Fig. 3(a) represents the original state when the optical power is zero and the relatively small deformation of this original state is caused only by the VWF. The static deformation increases with optical power and the deformation is elastic because the waveguide can return to its original state at A after the TGF is removed.

However, the two intersections approach when the optical power increases and coincide with each other [B in Fig. 3(a)] at a critical power. The solid black line cannot cross the dashed colored line above B. When the optical power slightly increases above the critical power ($P_c$) at B, the total force (TGF + VWF) increases too fast and becomes too large for the beam to achieve a stable deformation, and then the beam is pulled straight down to the substrate and the middle part of the beam is bonded to the surface. The final $D_{max}$ is as large as the designed gap (80 nm). More parts of the beam will be collapsed into the substrate surface if the optical power further increases. However, the deformation is plastic and irreversible and the waveguide is permanently bonded on the substrate by the ultrastrong VWF, even after the TGF is removed.

If we only consider the TGF as shown in Fig. 3(b), there is also a critical power $P_c$. When $P > P_c$, there is no stable solution and the waveguide will be pull down to the substrate. However, due to no VWF, it is always elastic and can return after the optical power decreases to zero.

The optically activated plastic and elastic behavior is very interesting, but it also limits the power lever in the waveguide. The above method can be implemented to roughly obtain...
FIG. 3. (Color online) The force-deformation response at the simplest case of an assumed uniform load (the solid black lines) and the averaged force for different optical input power at a given shape $u(x) = -D_{\text{max}}(2/L)^4x^2(x-L)^2$ (the dashed colored lines) when considering (a) TGF + VWF and (b) TGF only. In (a), the left intersection is the approximate stable solution at specific optical power. The intersection A represents the original shape caused by the VWF when the optical power is zero. B is the critical point above which the solid black line cannot cross the dashed colored line and there is no stable solution. In order to get the exact value, the iterative feedback tuning method has to be employed to get a convergence result. Using this method, we accurately calculate the $D_{\text{max}}$ at the center of the waveguide under different input optical power. Figure 4(a) shows the evolution of deformation shape versus the optical power by the total force (TGF + VWF). When $P = 0$, the waveguide is deflected only a little by the VWF, and then deflected more with increased power. As $P$ is at the critical power of 18.3 mW, it achieves a critical state, and it still can be recoverable after the stress is removed and returns to the original state at $P = 0$.

However, the waveguide will irreversibly be pulled to the substrate quickly when $P > P_c$. More parts of the beam will be collapsed into the substrate surface if the optical power further increases and the waveguide cannot return to its original shape even though the optical power is reduced to zero. The red shaded area is the plastic deformation range. Here we have to mention that the waveguide material is still in its elastic region.

If we only consider the TGF, there is also a critical power at 25.5 mW, but the waveguide can return to the original state at $P = 0$.

Figure 5(a) shows the curve of the final $D_{\text{max}}$ versus the optical power, for the TGF, the VWF, and TGF + VWF, respectively. The final $D_{\text{max}}$ for TGF + VWF is almost linear to the optical power if $P \ll P_c$. The critical state in this figure shows that there exists a critical power above which there is no stable solution of Eq. (6) and the waveguide is pulled straight down onto the substrate. The deformation is elastic in the absence of the VWF (the hollow square), and the waveguide can return to its initial shape when the power is reduced to

![Graph showing force-deformation response](image)

FIG. 4. (Color online) The evolution of the deformation shape versus the optical power by (a) the total force (TGF + VWF) and (b) TGF only. The white and red shaded areas are the elastic and plastic deformation range, respectively.
zero. However, the deformation is plastic when taking the VWF into consideration (the red circle); there exists a lower critical power above which the waveguide is pulled down to the substrate and permanently bonded to it. Another thing has to be mentioned is that the difference between $D_{\text{maxTGF+VWF}}$ and $D_{\text{maxTGF}}+D_{\text{maxVWF}}$ is always positive, and increases when the optical power increases.

We also calculate the critical power at different waveguide lengths for TGF + VWF. As shown in Fig. 5(b), $P_c$ is higher with a shorter waveguide and it has a nearly linear growth when the gap is above a critical value.

In this paper, we theoretically investigate the VWF’s influences on the NW optomechanical system consisting of a suspended silicon waveguide and a silica substrate. The calculation results show that the VWF has a great influence on the device performance by deforming the waveguides and thus tuning their effective refractive indices. When the input optical power is relatively low, the VWF would be larger or comparable to the TGF, whereas when the input power is relatively high, the interaction between the VWF and the TGF could make the VWF even larger than the TGF after the deformation.

Due to the unique property of the VWF, the NW deformation has the plastic and elastic behaviors depending on the input optical power. When the input optical power is above the critical power, the waveguide deformation is plastic and unrecoverable, even though the total force is less than the yield strength of the waveguide material. These interesting phenomena possibly pave the way for alternative applications of optomechanical devices. Finally, the results obtained in this work are also important and helpful for the design and operation of NW optomechanical devices.

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